

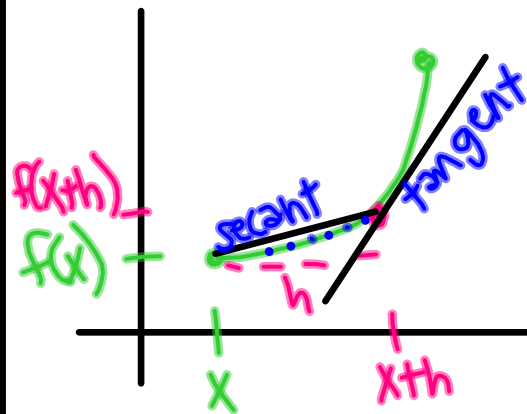
## 13.2 DEFINITION OF THE DERIVATIVE

ESSENTIAL QUESTION:

What is a derivative?

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tangent line - instantaneous rate of change.

Derivative is the slope of that line!

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

Notations:  $f'(x)$

$$\frac{dy}{dx}$$

$$\frac{d}{dx}$$

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~~ESSENTIAL QUESTION:~~ What is a derivative?

Derivative at a point

<http://goo.gl/efWfaP>

Derivative Graph Plotter

<http://goo.gl/iQyLNY>

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~~ESSENTIAL QUESTION:~~ What is a derivative?

ex.  $f(x) = 5x^2$ , find  $f'(x)$  and  $f'(3)$

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\lim_{h \rightarrow 0} \frac{5(x+h)^2 - 5x^2}{h}$$

$$\lim_{h \rightarrow 0} \frac{5(x^2 + 2xh + h^2) - 5x^2}{h}$$

$$\lim_{h \rightarrow 0} \frac{\cancel{5x^2} + 10xh + 5h^2 - \cancel{5x^2}}{h}$$

$$\lim_{h \rightarrow 0} \frac{\cancel{h}(10x + 5h)}{\cancel{h}}$$

$$\boxed{10x + 5(0)}$$

$$f'(x) = 10x$$

$$f'(3) = 10(3)$$

$$\boxed{30}$$