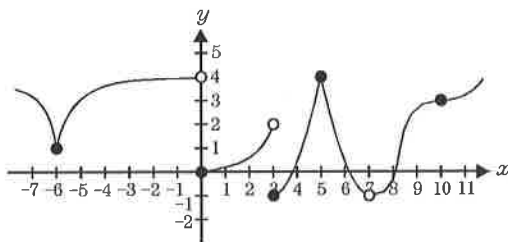


Name \_\_\_\_\_

Date \_\_\_\_\_

This figure shows the graph of  $f$ . Use this figure to answer the following question(s).



1. At which of the following  $x$ -values is  $f$  continuous? Choose the BEST answer.

I. -6  
 II. 0  
 III. 3  
 IV. 5  
 V. 7  
 VI. 10

a) I, II, and IV      b) IV and VI      c) I, IV, and VI      d) II, III, and V      e) I and IV

2. At which of the following  $x$ -values does  $f$  have a removeable discontinuity? Choose the BEST answer.

I. -6  
 II. 0  
 III. 3  
 IV. 5  
 V. 7  
 VI. 10

a) I, II, and IV      b) IV and VI      c) I, IV, and VI      d) II, III, and V      e) V only

3. At which of the following  $x$ -values does  $f$  have a jump discontinuity? Choose the BEST answer.

I. -6  
 II. 0  
 III. 3  
 IV. 5  
 V. 7  
 VI. 10

a) I, II, and IV      b) II only      c) I, IV, and VI      d) II, III, and V      e) V only

4. Given a function defined by  $f(x) = \frac{3x - 12}{x^2 - 6x + 8}$ , for what value(s) of  $x$  is the function discontinuous?
- a) 4 only                      b) 2                      c) 2, 4                      d) -4 only                      e) -4, -2
5. Which of the following functions are continuous for all real numbers  $x$ ?
- I.  $y = \frac{1}{x}$   
 II.  $y = 2^x$   
 III.  $y = \sec x$
- a) I and III only              b) II only                      c) II and III only              d) I and II only              e) I only
6. Given a function is defined by  $f(x) = \frac{2x + 2}{x^2 + 5x + 4}$ , for what value(s) of  $x$  does the function have one or more vertical asymptotes?
- a) 1 only                      b) -4 only                      c) -4 and -1                      d) 4 only                      e) 1 and 4
7. For what value(s) of  $x$  does the function defined by  $f(x) = \frac{x^2 - 6x + 8}{x^2 - 2x - 8}$  have a removeable discontinuity?
- a) 4 only                      b) 2 only                      c) -4 only                      d) 4 and -2                      e) -4 and 2
8. Let  $f$  be defined as follows:

$$f(x) = \begin{cases} \frac{x^2 - 9}{x - 3} & \text{for } x \neq 3, \\ 1 & \text{for } x = 3 \end{cases}$$

Which of the following are true about  $f$ ?

- I.  $\lim_{x \rightarrow 3} f(x)$  exists  
 II.  $f(3)$  exists  
 III.  $f(x)$  is continuous at  $x = 3$
- a) None                      b) I only                      c) II only                      d) I and II only                      e) I, II, and III
9. Let  $f$  be defined as follows:

$$f(x) = \begin{cases} \frac{x^2 - 64}{x - 8} & \text{for } x \neq 8, \\ 16 & \text{for } x = 8 \end{cases}$$

Which of the following are true about  $f$ ?

- I.  $\lim_{x \rightarrow 8} f(x)$  exists  
 II.  $f(8)$  exists  
 III.  $f(x)$  is continuous at  $x = 8$
- a) None                      b) I only                      c) II only                      d) I and II only                      e) I, II, and III

10. Let  $f$  be defined as follows:

$$f(x) = \begin{cases} \frac{x^2 - k^2}{x - k} & \text{for } x \neq k, \\ 1 & \text{for } x = k \end{cases}$$

Which of the following are true about  $f$ ?

- I.  $\lim_{x \rightarrow k} f(x)$  exists
- II.  $f(k)$  exists
- III.  $f(x)$  is continuous at  $x = k$

- a) None                      b) I only                      c) II only                      d) I and II only                      e) I, II, and III

11. Let  $f$  be defined as follows:

$$f(x) = \begin{cases} \frac{x^2 - k^2}{x - k} & \text{for } x \neq k, \\ 2k & \text{for } x = k \end{cases}$$

Which of the following are true about  $f$ ?

- I.  $\lim_{x \rightarrow k} f(x)$  exists
- II.  $f(k)$  exists
- III.  $f(x)$  is continuous at  $x = k$

- a) None                      b) I only                      c) II only                      d) I and II only                      e) I, II, and III

12. Consider the function

$$f(x) = \begin{cases} x^2 & \text{for } -2 < x < 2, \\ 4 & \text{for } x \geq 2, \\ 5 & \text{for } x \leq -2 \end{cases}$$

At  $x = -2$  the function has

- a) a jump discontinuity
- b) an infinite discontinuity
- c) a removable discontinuity
- d) a point at which the function is continuous
- e) a point at which the function is differentiable

13. Consider the function

$$f(x) = \begin{cases} x^2 + 5 & \text{for } x > 5, \\ 3ax & \text{for } x \leq 5 \end{cases}$$

For what value of  $a$  is the function continuous?

- a) 2                      b) 10                      c) 5                      d) 15                      e) 30

14. Consider  $f(x) = \begin{cases} x + c & \text{for } x < 3, \\ cx^2 + 5 & \text{for } x \geq 3 \end{cases}$

For what value of the constant  $c$  is  $f$  continuous for all real numbers?

BC Calculus      Continuity      4/11/2012

**Answer List**

- |       |                    |       |
|-------|--------------------|-------|
| 1. c  | 2. e               | 3. b  |
| 4. c  | 5. b               | 6. b  |
| 7. a  | 8. d               | 9. e  |
| 10. d | 11. e              | 12. a |
| 13. a | 14. $-\frac{1}{4}$ |       |

**Catalog List**

- |               |               |               |
|---------------|---------------|---------------|
| 1. APC CA 17  | 2. APC CA 19  | 3. APC CA 20  |
| 4. APC CF 1   | 5. APC CF 5   | 6. APC CF 13  |
| 7. APC CF 15  | 8. APC CF 17  | 9. APC CF 21  |
| 10. APC CF 25 | 11. APC CF 27 | 12. APC CF 29 |
| 13. APC CF 31 | 14. APC CF 45 |               |