

## 8.2 POLYNOMIAL OPERATIONS

Turn in the entire 8.1 HW (all 44 questions with work shown) right now!!!

## WARM-UP FRIDAY (in YOUR notes)

Without a calculator, find the quotient and remainder of the following problem.

$$8954762 \div 23$$

$$\begin{array}{r} 23 \\ \times 2 \\ \hline 46 \end{array} \quad \begin{array}{r} 23 \\ \times 3 \\ \hline 69 \end{array} \quad \begin{array}{r} 23 \\ \times 4 \\ \hline 92 \end{array} \quad \begin{array}{r} 23 \\ \times 5 \\ \hline 115 \end{array}$$
  
$$\begin{array}{r} 23 \\ \times 6 \\ \hline 138 \end{array} \quad \begin{array}{r} 23 \\ \times 7 \\ \hline 161 \end{array} \quad \begin{array}{r} 23 \\ \times 8 \\ \hline 184 \end{array} \quad \begin{array}{r} 23 \\ \times 9 \\ \hline 207 \end{array}$$

Handwritten long division of 2389337 by 23:

$$\begin{array}{r} 10389337 \text{ R } 11 \\ 23 \overline{) 8954762} \\ \underline{-69} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \\ 205 \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \\ \underline{-184} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \\ 214 \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \\ \underline{-207} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \\ 77 \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \\ \underline{-69} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \\ 7816 \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \\ \underline{-69} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \\ 172 \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \\ \underline{-161} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \\ 11 \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \phantom{0} \end{array}$$

# 8.2 POLYNOMIAL OPERATIONS

**EQ:** How do I determine the degree of a polynomial?

A **term** is an algebraic expression that can be written using constants, variables, multiplication and division.

The constants are called coefficients. <sup>ex.  $3x^2$</sup>  A **polynomial** can be written using terms and addition and subtraction. The term of the polynomial which does not include a variable is called the

constant term. Any letter may be used as the variable in a polynomial.

**Note the characteristics of a polynomial.**

- All exponents are whole numbers.
- No variables in the denominator.
- No variables under a radical.

Any letter may be used as the variable in a polynomial. Examples of **polynomials** include the following.

$$x^3 - 6x^2 + \frac{1}{2} \quad y^{15} + y^{10} + 7 \quad w - 6.7 \quad 12$$

~~$$x^3 - 6x^2 + \frac{1}{2}$$~~

~~$$\frac{1}{2x} + x^2$$~~

~~$$x^2 + \sqrt{x} + 2$$~~

# 8.2 POLYNOMIAL OPERATIONS

**EQ:** How do I determine the degree of a polynomial?

**Degree of a Polynomial** – The *exponent* of the highest power of  $x$  is the **degree** of the polynomial, and the coefficient of this highest power of the variable is the **leading coefficient**.

FOLled → biggest exponent

Polynomial	Degree <small>exp.</small>	Leading Coefficient <small>big #</small>	Constant Term
<u><math>6x^7 + 4x^3 + 5x^2 - 7x + 10</math></u>	7	6	10
$x^3$	3	1	0
$12x^0$	0	12 =	12
<u><math>2x^6 + 3x^7 - x^8 - 2x - 4</math></u>	8	-1	-4
$(x-3)^2(x+2)(x-7)^3$ $x^2 \cdot x^1 \cdot x^3$	$2+1+3=6$ 6	1	$(-3)^2(2)(-7)^3$ ☹

FACTORED → add exponents

# 8.2 POLYNOMIAL OPERATIONS

**EQ:** How do I determine the degree of a polynomial?

Polynomial functions of degree less than 5 are often referred to by special names.

- First-degree polynomial functions are called linear functions.
- Second-degree polynomial functions are called quadratic functions.
- Third-degree polynomial functions are called cubic functions.
- Fourth-degree polynomial functions are called quartic functions.

# 8.2 POLYNOMIAL OPERATIONS

**EQ:** How do I determine the degree of a polynomial?

*Adding and Subtracting Polynomials* To add or subtract polynomials, combine like terms

ex.  $(-2x^3 + x^2 - 4x) - (2x^3 - x + 4)$

DISTRIBUTE NEGATIVE

$$\begin{array}{r} -2x^3 + x^2 - 4x \quad -2x^3 + x - 4 \\ \hline -4x^3 + x^2 - 3x - 4 \end{array}$$

# 8.2 POLYNOMIAL OPERATIONS

**EQ:** How do I determine the degree of a polynomial?

*Multiplying Polynomials* To multiply polynomials, distribute/FOIL

ex.  $(2x-3)(x^2+3x-5)$

$$2x^3 + \underline{6x^2} - \underline{10x} - \underline{3x^2} - \underline{9x} + 15$$

$$\boxed{2x^3 + 3x^2 - 19x + 15}$$

Synthetic \* use when divisor is 1st degree binomial

$$(2x^3 + 3x - 5) \div (x - 2)$$

opposite sign  $\rightarrow$   $2 \mid 2 \ 0 \ 3 \ -5$   
 $\downarrow 4 \ 8 \ 22$   
 $2 \ 4 \ 11 \ 17 \leftarrow \text{remainder}$   
 $\boxed{2x^2 + 4x + 11 \ R \ 17}$

Synthetic basics

1. Bring down 1st #
2. Multiply
3. Add down column
4. Repeat for each column
5. Answer is one degree less

Don't forget the zeros for missing terms!

Long Division

$$(x^4 + 3x^3 - 2x^2 + x - 3) \div (x^2 + x - 2)$$

$$x^2 + 2x - 2 \ R \ 7x - 7$$

$$\begin{array}{r}
 x^2 + x - 2 \overline{) x^4 + 3x^3 - 2x^2 + x - 3} \\
 \underline{-(x^4 + 1x^3 + 2x^2)} \phantom{+ x - 3} \\
 2x^3 + 0x^2 + x \phantom{- 3} \\
 \underline{-(2x^3 + 2x^2 + 4x)} \phantom{- 3} \\
 -2x^2 + 5x - 3 \\
 \underline{+(2x^2 + 2x + 4)} \\
 7x - 7
 \end{array}$$

# 8.2 POLYNOMIAL OPERATIONS

**EQ:** How do I determine the degree of a polynomial?

**EXIT TICKET**

on google classroom



## 8.2—Operations with Polynomials

odds  
evens



Name \_\_\_\_\_

In Exercises 1 – 8 determine whether the given algebraic expression is a polynomial. If it is, list its leading coefficient, constant term, and degree.

1.  $1 + x^3$

2.  $7^x + 2x + 1$

3.  $(x + \sqrt{3})(x - \sqrt{3})$

4.  $4x^2 + 3\sqrt{x} + 5$

5.  $\frac{7}{x^2} + \frac{5}{x} - 15$

6.  $(x - 1)^k$   
where k is a fixed, positive integer

In Exercises 7 – 14 perform the indicated operations

7.  $(m^2 + 3) - (4 - 3m)$

8.  $(2x^2 - 4x + 7) - (-2x^2 + 3x - 7)$

9.  $5a^4(a^2 - 4a + 3)$

10.  $(x + 2)(x^2 - 4x + 5)$

11.  $(7x - 3)^2$

12.  $(5 - 2x)^2$

13.  $(2x + 5)(2x - 5) - (2x + 5)^2$

14.  $(x + 3)^2 + (x - 3)^2$

In Exercises 15 – 19, use synthetic division to find the quotient and remainder.

15.  $(3x^4 - 8x^3 + 9x + 5) \div (x - 2)$

16.  $(4x^3 - 3x^2 + x + 7) \div (x - 2)$

17.  $(3x^3 - 2x^2 - 8) \div (x + 5)$

18.  $(2x^4 + 5x^3 - 2x - 8) \div (x + 3)$

19.  $(x^6 - x^5 + x^4 - x^3 + x^2 - x + 1) \div (x - 1)$

In Exercises 20 – 22, state the quotient and remainder when the first polynomial is divided by the second using long division. Check your division by calculating: (Divisor)(Quotient) + Remainder.

20.  $3x^4 + 2x^2 - 6x + 1$ ;  $x + 1$

21.  $3x^4 - 3x^3 - 11x^2 + 6x - 1$ ;  $x^3 + x^2 - 2$

22.  $x^5 - 1$ ;  $x - 1$

## 8.2 POLYNOMIAL OPERATIONS

**EQ:** How do I determine the degree of a polynomial?

### *Dividing Polynomials*

**Ex.**  $(3x^4 - 8x^2 - 11x + 1) \div (x - 2)$

#### **Synthetic Division**

Only works when divisor is first degree binomial

#### Synthetic basics

1. Bring down 1st #
2. Multiply
3. Add down column
4. Repeat for each column
5. Answer is one degree less

Don't forget the zeros for missing terms!

#### **Long Division**

to check your answer...

$$\text{answer} * \text{divisor} + \text{remainder} = \text{original}$$