

9.4 Solving Log Equations

Essential Question

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Method 1. CONDENSE.

$$\text{ex. } \log_3 x = 2\log_3 4 - \log_3 2$$

$$\log_3 x = \log_3 16 - \log_3 2$$

$$\log_3 x = \log_3 (8)$$

$$\boxed{x = 8}$$

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Method 2. Rewrite in exponential form.

$$\text{ex. } \log_3(2x - 3) = 2$$

$$\log_b a = x \Leftrightarrow b^x = a$$

$$3^2 = 2x - 3$$

$$9 = 2x - 3$$

$$12 = 2x$$

$$\boxed{6 = x}$$

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Method 3. Combine method 1 & 2.

ex. $\log(x+2) + \log(x-1) = 1$

$$\log_{10}((x+2)(x-1)) = 1$$

$$10^1 = (x+2)(x-1)$$

$$10 = x^2 + x - 2$$

$$0 = x^2 + x - 12$$

$$(x-3)(x+4)$$

$$x=3$$

$$x \cancel{=} -4$$

Argument
of log
can never
be neg!

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Method 4. Rewrite with the same base or as a log
or take the log of both sides.

ex. $3^{x+2} = 7$

$$\begin{aligned} \log_3 7 &= x+2 \\ \log_3 7 - 2 &= x \quad \checkmark \end{aligned}$$

$$\log_3^{x+2} = \log_3 7$$

$$(x+2) \log_3 = \log_3 7$$

$$\log_3$$

$$x+2 = \frac{\log_3}{\log_3}$$

$$-2 \quad -2$$

ex. $3^{x+2} = q$

$$\begin{aligned} 3^{x+2} &= 3^2 \\ x+2 &= 2 \end{aligned}$$