

Compound Inequalities

Agenda

Warm-Up

HW Check

Notes

Homework:
Practice

Objective: You
will recognize
and solve
compound
inequalities.

Warm-Up

Write the inequality and solve.

1. Four is less than or equal to twice a number plus twelve.

$$\begin{array}{r}
 4 \leq 2x + 12 \\
 -12 \quad -12 \\
 \hline
 -8 \leq 2x \\
 \frac{-8}{2} \leq \frac{2x}{2} \\
 -4 \leq x
 \end{array}$$

2. Twice a number increased by 10 is at most 12 less than the same number.

$$\begin{array}{r}
 2x + 10 \leq x - 12 \\
 -x \quad -x \\
 \hline
 x + 10 \leq -12 \\
 -10 \quad -10 \\
 \hline
 x \leq -22
 \end{array}$$

$$12 < x$$

Homework Check

Did you hear about....

1 2 3 4 5 6 7 8 9
The girl and guy who met in a revolving
door and started going around together??
10 11 12 13 14 15

Did You Hear About . . .

1 The	2 girl	3 3	4 guy	5 who	6 met	7 in	8 a
9 rev.	10 door	11 3	12 3	13 3	14 3	15 3	??

Solve each inequality or problem. Write the word under the correct solution in the box containing the exercise number.

Answers 1-7

$x \geq 44$	OFTEN
$x \leq -2\frac{1}{2}$	AND
$x > 15$	HER
$x > 4\frac{1}{3}$	THE
$x < -7$	MONKEYS
$x > 13$	GUY
$x \geq 58$	MET
$x \geq 8$	WHEN
$x \leq -2$	GIRL
$x \geq 5$	IN
$x \leq -4\frac{2}{3}$	FRIENDS
$x < -4$	WHO

- $7x + 2 > 4x + 15$
- $10 - 3x \geq 5x + 26$
- $9x + 40 \leq 15 - x$
- $3(x - 7) > 18$
- $75 < -5(4x + 1)$
- $6(2x - 9) \geq 4 + 11x$
- $8 - 3(4x - 1) \leq -49$

15 Suppose you write a book. The printer charges \$4 per book to print it, and you spend \$3500 on advertising. You sell the book for \$15 a copy. How many copies must you sell so that your income from sales is greater than your total cost?

Answers 8-15

$t > -1\frac{3}{4}$	DOOR
$t < 8$	SPINNING
$t \leq 0$	AROUND
≥ 308	CIRCLES
$t \leq 25$	REVOLVING
$t \geq -1$	STARTED
$t \leq 3\frac{1}{3}$	IN
≥ 319	TOGETHER
$t < 5$	AND
$t > -6\frac{1}{5}$	A
$t < 4\frac{1}{2}$	GOING
$t \geq -3$	DIZZY

8 $2(t+5) > 4t - 7(t+3)$
 $2t+10 > 4t-7t-21$
 $2t+10 > -3t-21$
 $+3t$
 $5t+10 > -21$
 -10
 $5t > -31$
 10 $14 - (9t-2) < -t+26$
 $14-9t+2 < -t+26$
 $16-9t < -t+26$
 $+9t$
 $16 < -t+26$
 $+t$
 $16 < 25$
 13 $7(5t-4) - 12 + 15t < 60$
 $35t-28-12+15t < 60$
 $50t-40 < 60$
 $+40$
 $50t < 100$
 $\div 50$
 $t < 2$
 14 $9(9t-4) + 13(12-3t) > 30$
 $81t-36+156-39t > 30$
 $42t+120 > 30$
 -120
 $42t > -90$
 $\div 42$
 $t > -2\frac{1}{7}$

Inequalities:
Solving Inequalities With Parentheses and/or the Variable on Both Sides

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15-4
 $(15-4)x$
 $11x > 3500$
 $\div 11$
 $x > 319$ books

p.22

Algebra I - Unit 1: Topic 4 - Compound Inequalities

Student Notes - Compound Inequalities

pp 202-208

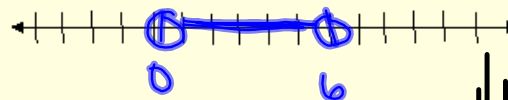
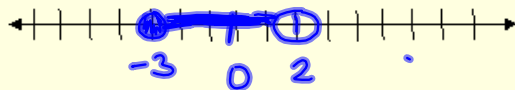
Compound inequality:

- when 2 inequalities are combined into 1 statement

Graph the compound inequality:

1. $-3 \leq x < 2$

2. $0 < x < 6$



Solve the compound inequality and graph the solutions.

3. $4 \leq x + 2 \leq 8$

$$\begin{array}{r} -2 \quad -2 \quad -2 \\ \hline 2 \leq x \leq 6 \end{array}$$



4. $-5 \leq 2x + 3 \leq 9$

$$\begin{array}{r} -3 \quad -3 \quad -3 \\ \hline -8 \leq 2x \leq 6 \\ \hline 2 \quad 2 \quad 2 \\ \hline -4 \leq x \leq 3 \end{array}$$

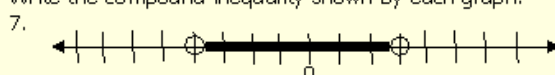


5. Jimmy's car can travel between 380 and 410 miles, inclusive, on a full tank of gas. He filled his tank of and drove 45 miles. How many more miles can he drive without running out of gas?

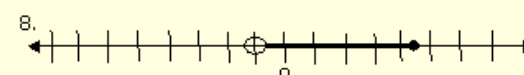
$$\begin{array}{r} 380 \leq x + 45 \leq 410 \\ -45 \quad -45 \quad -45 \\ \hline 335 \leq x \leq 365 \end{array}$$

He can drive between 335 and 365 more miles.

Write the compound inequality shown by each graph.



$$-4 < x < 3$$



$$-1 < x \leq 4.5$$

REVIEW

Solve for the given variable.

9. Solve for y on $3x + 7y = 2$

$$\begin{array}{r} -3x \quad -3x \\ \hline 7y = 2 - 3x \\ \hline 7 \quad 7 \\ \hline y = \frac{2 - 3x}{7} \\ \hline y = \frac{2}{7} - \frac{3}{7}x \end{array}$$

10. Solve for f on $\frac{f+3}{g} = 10$

Algebra I - Unit 1: Topic 4 – Compound Inequalities

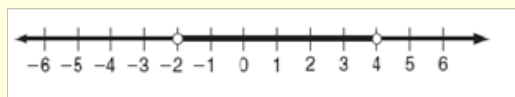
Practice: Compound Inequalities

pp 202-205

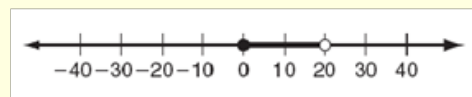
Name _____ Date _____ Per _____

Write the compound inequality shown by each graph.

1.



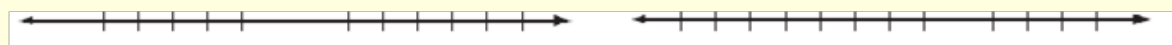
2.



Solve each compound inequality and graph the solutions.

3. $-15 < x - 8 < -4$

4. $12 \leq 4n < 28$



5. $-2 \leq 3b + 7 \leq 13$

6. $5 < 3x - 1 < 17$



Algebra I - Unit 1: Topic 4 – Compound Inequalities

Write a compound inequality for each problem. Graph the solutions.

7. The temperature in a pet iguana's cage should be between 70°F and 95°F , inclusive.

~~8. Water is a liquid if its temperature is less than 100°C and greater than 0°C .~~

8. A tropical fish requires a water temperature between 68°F and 77°F , inclusive. An aquarium is heated 8 degrees so that a Tetra can live in it. What temperatures could the water have been before the heating?

~~10. Nathan will be working between 30 to 39 hours, inclusive, this week which is triple what he worked last week. How many hours did Nathan work last week?~~

9. Which of the following is a solution of $-1 < x - 3 < 2$?

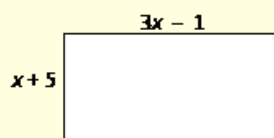
A 2

B 3

C -2

D 5

10. The perimeter of the rectangle is 80 m. Find the value of x and the value of each side.



$x =$ _____

Side lengths: _____

