

Vectors Day 2

Essential Question

How do I calculate the angle
between two vectors?

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~~The Dot Product~~

$$u \bullet v = a_1 a_2 + b_1 b_2$$

ex. $u = \underline{2}i + \underline{1}j$, $v = \underline{5}i - \underline{6}j$

$$u \bullet v = 2(5) + 1(-6) = 10 - 6 = \boxed{4}$$

*Two vectors are orthogonal (perpendicular) if $u \bullet v = 0$

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Essential Question How do I calculate the angle between two vectors?

~~Angle between 2 vectors~~ Dot Product Theorem

$$u \bullet v = \|u\| \|v\| \cos \theta$$

To find an angle... $\cos \theta = \frac{u \bullet v}{\|u\| \|v\|}$

ex. $u=4i-3j$ and $v=2i+5j$

$$u \bullet v = 4(2) + (-3)(5) = 8 - 15 = -7$$

$$\|u\| = \sqrt{4^2 + (-3)^2} = 5$$

$$\|v\| = \sqrt{2^2 + 5^2} = \sqrt{29}$$

$$\theta = \cos^{-1} \left(\frac{-7}{5\sqrt{29}} \right)$$

degrees

105°