

→ one Δ

ANGLE → two Δs

4.4 Composition of Trig Values use restricted ranges!

Name: _____

Find the exact values of each expression using radicals or radians if necessary.

1. $\tan\left(\cos^{-1}\left(\frac{4}{5}\right)\right)$



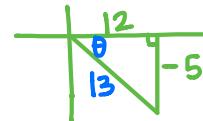
$$\begin{aligned}4^2 + y^2 &= 5^2 \\16 + y^2 &= 25 \\y^2 &= 9 \\y &= 3\end{aligned}$$

2. $\cos\left(\arctan\left(\frac{4}{3}\right)\right)$

$$\cos\left(\tan^{-1}\left(\frac{4}{3}\right)\right)$$

$$\boxed{\frac{3}{5}}$$

3. $\sin\left(\tan^{-1}\left(-\frac{5}{12}\right)\right)$



$$\sin \theta = \frac{\text{OPP}}{\text{HYP}}$$

$$\boxed{-\frac{5}{13}}$$

$$\begin{aligned}12^2 + (-5)^2 &= c^2 \\144 + 25 &= c^2 \\169 &= c^2 \\13 &= c\end{aligned}$$

4. $\sec\left(\arcsin\left(-\frac{4}{7}\right)\right)$

$$\boxed{\frac{7}{\sqrt{33}}}$$

ANGLE 5. $\sin^{-1}\left(\cos(0)\right)$

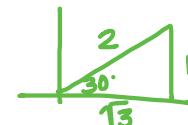


$$\cos 0 = 1$$

$\sin^{-1}(1)$
where does $y = 1$?

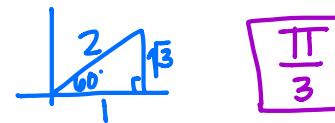
$$\boxed{\frac{\pi}{2}}$$

ANGLE 6. $\arccos\left(\sin\left(\frac{\pi}{6}\right)\right) \quad \frac{\pi}{6} = 30^\circ$



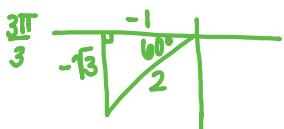
$$\sin \frac{\pi}{6} = \frac{1}{2}$$

$$\cos^{-1}\left(\frac{1}{2}\right)$$



$$\boxed{\frac{\pi}{3}}$$

ANGLE 7. $\cos^{-1}\left(\sin\left(\frac{4\pi}{3}\right)\right)$



$$\sin \frac{4\pi}{3} = -\frac{\sqrt{3}}{2}$$

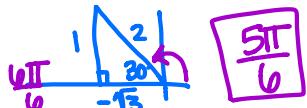
$$\cos^{-1}\left(-\frac{\sqrt{3}}{2}\right) \text{ QII}$$

8. $\cot\left(\csc^{-1}\left(-\frac{5}{3}\right)\right)$

$$\boxed{-\frac{4}{3}}$$

ANGLE 9. $\sin^{-1}\left(\cos\left(\frac{7\pi}{6}\right)\right)$

$$\boxed{-\frac{\pi}{3}}$$



$$\boxed{\frac{5\pi}{6}}$$

ANGLE 10. $\tan^{-1}(\cos(\pi))$

$$-\frac{\pi}{4}$$

ANGLE 11. $\tan^{-1}\left(\tan\left(-\frac{4\pi}{3}\right)\right)$

12. $\cos\left(\arcsin\left(-\frac{\sqrt{3}}{5}\right)\right)$

$$\frac{\sqrt{22}}{5}$$

13. $\sin\left(\sec^{-1}\left(-\frac{4}{3}\right)\right)$

$$\frac{\sqrt{17}}{4}$$

ANGLE 14. $\text{arcsec}\left(\sec\left(-\frac{\pi}{3}\right)\right)$

$$\frac{\pi}{3}$$

ANGLE 15. $\sin^{-1}\left(\cot\left(\frac{3\pi}{4}\right)\right)$

$$-\frac{\pi}{2}$$

16. $\tan\left(\text{arcsec}\left(-\sqrt{2}\right)\right)$

$$-1$$

17. $\sin\left(\sec^{-1}(-4)\right)$

$$\frac{\sqrt{15}}{4}$$

18. $\sec\left(\csc^{-1}(-3)\right)$

$$\frac{3}{18}$$

19. $\csc\left(\cot^{-1}(2)\right)$

$$\sqrt{15}$$

ANGLE 20. $\arcsin(\cos(\pi))$

$$-\frac{\pi}{2}$$

21. $\tan\left(\sin^{-1}\left(-\frac{7}{5}\right)\right)$

hypotenuse should be longest side.

NO SOLUTION